

## Chapter 10

# Cluster Analysis: Basic Concepts and Methods

### 10.1 Bibliographic Notes

Clustering has been extensively studied for over 40 years and across many disciplines due to its broad applications. Most books on pattern classification and machine learning contains chapters on cluster analysis or unsupervised learning. Several textbooks are dedicated to the methods of cluster analysis, including Hartigan [Har75], Jain and Dubes [JD88], Kaufman and Rousseeuw [KR90], and Arabie, Hubert, and De Sorte [AHS96]. There are also many survey articles on different aspects of clustering methods. Recent ones include Jain, Murty, and Flynn [JMF99], Parsons, Haque, and Liu [PHL04], and Jain [Jai10].

For partitioning methods, the  $k$ -means algorithm was first introduced by Lloyd [Llo57], and then by MacQueen [Mac67]. Arthur and Vassilvitskii [AV07] presented the  $k$ -means++ algorithm. A filtering algorithm, which uses a spatial hierarchical data index to speed up the computation of cluster means, is given in Kanungo, Mount, Netanyahu, Piatko, Silverman, and Wu [KMN<sup>+</sup>02].

The  $k$ -medoids algorithms of PAM and CLARA were proposed by Kaufman and Rousseeuw [KR90]. The  $k$ -modes (for clustering nominal data) and  $k$ -prototypes (for clustering hybrid data) algorithms were proposed by Huang [Hua98]. The  $k$ -modes clustering algorithm was also proposed independently by Chaturvedi, Green, and Carroll [CGC94, CGC01]. The CLARANS algorithm was proposed by Ng and Han [NH94]. Ester, Kriegel, and Xu [EKX95] proposed techniques for further improvement of the performance of CLARANS using efficient spatial access methods, such as R\*-tree and focusing techniques. A  $k$ -means-based scalable clustering algorithm was proposed by Bradley, Fayyad, and Reina [BFR98].

An early survey of agglomerative hierarchical clustering algorithms was conducted by Day and Edelsbrunner [?]. Agglomerative hierarchical clustering, such as AGNES, and divisive hierarchical clustering, such as DIANA, were in-

roduced by Kaufman and Rousseeuw [KR90]. An interesting direction for improving the clustering quality of hierarchical clustering methods is to integrate hierarchical clustering with distance-based iterative relocation or other non-hierarchical clustering methods. For example, BIRCH, by Zhang, Ramakrishnan, and Livny [ZRL96], first performs hierarchical clustering with a CF-tree before applying other techniques. Hierarchical clustering can also be performed by sophisticated linkage analysis, transformation, or nearest neighbor analysis, such as CURE by Guha, Rastogi, and Shim [GRS98], ROCK (for clustering nominal attributes) by Guha, Rastogi, and Shim [GRS99], and Chameleon by Karypis, Han, and Kumar [KHK99].

A probabilistic hierarchical clustering framework following normal linkage algorithms and using probabilistic models to define cluster similarity was developed by Friedman [Fri03], and Heller and Ghahramani [HG05].

For density-based clustering methods, DBSCAN was proposed by Ester, Kriegel, Sander, and Xu [EKSX96]. Ankerst, Breunig, Kriegel, and Sander [ABKS99] developed OPTICS, a cluster ordering method that facilitates density-based clustering without worrying about parameter specification. The DENCLUE algorithm, based on a set of density distribution functions, was proposed by Hinneburg and Keim [HK98]. Hinneburg and Gabriel [HG07] developed DENCLUE 2.0 which includes a new hill climbing procedure for Gaussian kernels adjusting the step size automatically.

STING, a grid-based multiresolution approach that collects statistical information in grid cells, was proposed by Wang, Yang, and Muntz [WYM97]. WaveCluster, developed by Sheikholeslami, Chatterjee, and Zhang [SCZ98], is a multiresolution clustering approach that transforms the original feature space by wavelet transform.

Scalable methods for clustering nominal data were studied by Gibson, Kleinberg, and Raghavan [GKR98], by Guha, Rastogi, and Shim [GRS99], and by Ganti, Gehrke, and Ramakrishnan [GGR99]. There are also many other clustering paradigms. For example, fuzzy clustering methods are discussed in Kaufman and Rousseeuw [KR90], in Bezdek [Bez81], and in Bezdek and Pal [BP92].

For high-dimensional clustering, an Apriori-based dimension-growth subspace clustering algorithm called CLIQUE was proposed by Agrawal, Gehrke, Gunopulos, and Raghavan [AGGR98]. It integrates density-based and grid-based clustering methods.

Recent studies have proceeded to clustering stream data [BBD<sup>+</sup>02]. A  $k$ -median based data stream clustering algorithm was proposed by Guha, Mishra, Motwani, and O'Callaghan [GMMO00], and by O'Callaghan et al. [OMM<sup>+</sup>02]. A method for clustering evolving data streams was proposed by Aggarwal, Han, Wang, and Yu [AHWY03]. A framework for projected clustering of high-dimensional data streams was proposed by Aggarwal, Han, Wang, and Yu [AHWY04].

Clustering evaluation is discussed in a few monographs and survey articles, such as [JD88, HBV01]. The extrinsic methods for clustering quality evaluation are extensively explored. Some recent studies include [Mei03, Mei05, AGAV09]. The four essential criteria introduced in this chapter are formulated

in [AGAV09], while some individual criteria are also mentioned earlier, for example, in [Mei03, RH07]. Bagga and Baldwin [BB98] introduced the BCubed metrics. The silhouette coefficient is described in [KR90].



# Bibliography

- [ABKS99] M. Ankerst, M. Breunig, H.-P. Kriegel, and J. Sander. OPTICS: Ordering points to identify the clustering structure. In *Proc. 1999 ACM-SIGMOD Int. Conf. Management of Data (SIGMOD'99)*, pages 49–60, Philadelphia, PA, June 1999.
- [AGAV09] E. Amigó, J. Gonzalo, J. Artilles, and F. Verdejo. A comparison of extrinsic clustering evaluation metrics based on formal constraints. *Information Retrieval*, 12, 2009.
- [AGGR98] R. Agrawal, J. Gehrke, D. Gunopulos, and P. Raghavan. Automatic subspace clustering of high dimensional data for data mining applications. In *Proc. 1998 ACM-SIGMOD Int. Conf. Management of Data (SIGMOD'98)*, pages 94–105, Seattle, WA, June 1998.
- [AHS96] P. Arabie, L. J. Hubert, and G. De Soete. *Clustering and Classification*. World Scientific, 1996.
- [AHWY03] C. C. Aggarwal, J. Han, J. Wang, and P. S. Yu. A framework for clustering evolving data streams. In *Proc. 2003 Int. Conf. Very Large Data Bases (VLDB'03)*, pages 81–92, Berlin, Germany, Sept. 2003.
- [AHWY04] C. C. Aggarwal, J. Han, J. Wang, and P. S. Yu. A framework for projected clustering of high dimensional data streams. In *Proc. 2004 Int. Conf. Very Large Data Bases (VLDB'04)*, pages 852–863, Toronto, Canada, Aug. 2004.
- [AV07] D. Arthur and S. Vassilvitskii. K-means++: The advantages of careful seeding. In *Proc. 2007 ACM-SIAM Symp. Discrete Algorithms (SODA'07)*, pages 1027–1035, Tokyo, Japan, 2007.
- [BB98] A. Bagga and B. Baldwin. Entity-based cross-document coreferencing using the vector space model. In *Proc. 1998 Annual Meeting of the Association for Computational Linguistics and Int. Conf. Computational Linguistics (COLING-ACL'98)*, Montreal, Canada, Aug. 1998.

- [BBD<sup>+</sup>02] B. Babcock, S. Babu, M. Datar, R. Motwani, and J. Widom. Models and issues in data stream systems. In *Proc. 2002 ACM Symp. Principles of Database Systems (PODS'02)*, pages 1–16, Madison, WI, June 2002.
- [Bez81] J. C. Bezdek. *Pattern Recognition with Fuzzy Objective Function Algorithms*. Plenum Press, 1981.
- [BFR98] P. Bradley, U. Fayyad, and C. Reina. Scaling clustering algorithms to large databases. In *Proc. 1998 Int. Conf. Knowledge Discovery and Data Mining (KDD'98)*, pages 9–15, New York, NY, Aug. 1998.
- [BP92] J. C. Bezdek and S. K. Pal. *Fuzzy Models for Pattern Recognition: Methods That Search for Structures in Data*. IEEE Press, 1992.
- [CGC94] A. Chaturvedi, P. Green, and J. Carroll. K-means, k-medians and k-modes: Special cases of partitioning multiway data. In *The Classification Society of North America (CSNA) Meeting Presentation*, Houston, TX, 1994.
- [CGC01] A. Chaturvedi, P. Green, and J. Carroll. K-modes clustering. *J. Classification*, 18:35–55, 2001.
- [EKSX96] M. Ester, H.-P. Kriegel, J. Sander, and X. Xu. A density-based algorithm for discovering clusters in large spatial databases. In *Proc. 1996 Int. Conf. Knowledge Discovery and Data Mining (KDD'96)*, pages 226–231, Portland, OR, Aug. 1996.
- [EKX95] M. Ester, H.-P. Kriegel, and X. Xu. Knowledge discovery in large spatial databases: Focusing techniques for efficient class identification. In *Proc. 1995 Int. Symp. Large Spatial Databases (SSD'95)*, pages 67–82, Portland, ME, Aug. 1995.
- [Fri03] N. Friedman. Pcluster: Probabilistic agglomerative clustering of gene expression profiles. In *Technical Report 2003-80, Hebrew Univ.*, 2003.
- [GGR99] V. Ganti, J. E. Gehrke, and R. Ramakrishnan. CACTUS—clustering categorical data using summaries. In *Proc. 1999 Int. Conf. Knowledge Discovery and Data Mining (KDD'99)*, pages 73–83, San Diego, CA, 1999.
- [GKR98] D. Gibson, J. M. Kleinberg, and P. Raghavan. Clustering categorical data: An approach based on dynamical systems. In *Proc. 1998 Int. Conf. Very Large Data Bases (VLDB'98)*, pages 311–323, New York, NY, Aug. 1998.
- [GMMO00] S. Guha, N. Mishra, R. Motwani, and L. O'Callaghan. Clustering data streams. In *Proc. 2000 Symp. Foundations of Computer Science (FOCS'00)*, pages 359–366, Redondo Beach, CA, 2000.

- [GRS98] S. Guha, R. Rastogi, and K. Shim. CURE: An efficient clustering algorithm for large databases. In *Proc. 1998 ACM-SIGMOD Int. Conf. Management of Data (SIGMOD'98)*, pages 73–84, Seattle, WA, June 1998.
- [GRS99] S. Guha, R. Rastogi, and K. Shim. ROCK: A robust clustering algorithm for categorical attributes. In *Proc. 1999 Int. Conf. Data Engineering (ICDE'99)*, pages 512–521, Sydney, Australia, Mar. 1999.
- [Har75] J. A. Hartigan. *Clustering Algorithms*. John Wiley & Sons, 1975.
- [HBV01] M. Halkidi, Y. Batistakis, and M. Vazirgiannis. On clustering validation techniques. *J. Intell. Inf. Syst.*, 17:107–145, 2001.
- [HG05] K. A. Heller and Z. Ghahramani. Bayesian hierarchical clustering. In *Proc. 22nd Int. Conf. Machine Learning (ICML'05)*, pages 297–304, Bonn, Germany, 2005.
- [HG07] A. Hinneburg and H.-H. Gabriel. DENCLUE 2.0: Fast clustering based on kernel density estimation. In *Proc. 2007 Int. Conf. Intelligent Data Analysis (IDA'07)*, pages 70–80, Ljubljana, Slovenia, 2007.
- [HK98] A. Hinneburg and D. A. Keim. An efficient approach to clustering in large multimedia databases with noise. In *Proc. 1998 Int. Conf. Knowledge Discovery and Data Mining (KDD'98)*, pages 58–65, New York, NY, Aug. 1998.
- [Hua98] Z. Huang. Extensions to the  $k$ -means algorithm for clustering large data sets with categorical values. *Data Mining and Knowledge Discovery*, 2:283–304, 1998.
- [Jai10] A. K. Jain. Data clustering: 50 years beyond  $k$ -means. *Pattern Recognition Lett.*, 31, 2010.
- [JD88] A. K. Jain and R. C. Dubes. *Algorithms for Clustering Data*. Prentice Hall, 1988.
- [JMF99] A. K. Jain, M. N. Murty, and P. J. Flynn. Data clustering: A survey. *ACM Comput. Surv.*, 31:264–323, 1999.
- [KHK99] G. Karypis, E.-H. Han, and V. Kumar. CHAMELEON: A hierarchical clustering algorithm using dynamic modeling. *COMPUTER*, 32:68–75, 1999.
- [KMN<sup>+</sup>02] T. Kanungo, D. M. Mount, N. S. Netanyahu, C. D. Piatko, R. Silverman, and A. Y. Wu. An efficient  $k$ -means clustering algorithm: Analysis and implementation. *IEEE Trans. Pattern Analysis and Machine Intelligence (PAMI)*, 24:881–892, 2002.

- [KR90] L. Kaufman and P. J. Rousseeuw. *Finding Groups in Data: An Introduction to Cluster Analysis*. John Wiley & Sons, 1990.
- [Llo57] S. P. Lloyd. Least squares quantization in PCM. *IEEE Trans. Information Theory*, 28:128–137, 1982 (original version: Technical Report, Bell Labs, 1957).
- [Mac67] J. MacQueen. Some methods for classification and analysis of multivariate observations. *Proc. 5th Berkeley Symp. Mathematical Statistics and Probability*, 1:281–297, 1967.
- [Mei03] M. Meilă. Comparing clusterings by the variation of information. In *Proc. 16th Annual Conf. Computational Learning Theory (COLT'03)*, pages 173–187, Washington, DC, Aug. 2003.
- [Mei05] M. Meilă. Comparing clusterings: an axiomatic view. In *Proc. 22nd Int. Conf. Machine Learning (ICML'05)*, pages 577–584, Bonn, Germany, 2005.
- [NH94] R. Ng and J. Han. Efficient and effective clustering method for spatial data mining. In *Proc. 1994 Int. Conf. Very Large Data Bases (VLDB'94)*, pages 144–155, Santiago, Chile, Sept. 1994.
- [OMM<sup>+</sup>02] L. O'Callaghan, A. Meyerson, R. Motwani, N. Mishra, and S. Guha. Streaming-data algorithms for high-quality clustering. In *Proc. 2002 Int. Conf. Data Engineering (ICDE'02)*, pages 685–696, San Francisco, CA, Apr. 2002.
- [PHL04] L. Parsons, E. Haque, and H. Liu. Subspace clustering for high dimensional data: A review. *SIGKDD Explorations*, 6:90–105, 2004.
- [RH07] A. Rosenberg and J. Hirschberg. V-measure: A conditional entropy-based external cluster evaluation measure. In *Proc. 2007 Joint Conf. on Empirical Methods in Natural Language Processing and Computational Natural Language Learning (EMNLP-CoNLL'07)*, pages 410–420, Prague, Czech Republic, June 2007.
- [SCZ98] G. Sheikholeslami, S. Chatterjee, and A. Zhang. WaveCluster: A multi-resolution clustering approach for very large spatial databases. In *Proc. 1998 Int. Conf. Very Large Data Bases (VLDB'98)*, pages 428–439, New York, NY, Aug. 1998.
- [WYM97] W. Wang, J. Yang, and R. Muntz. STING: A statistical information grid approach to spatial data mining. In *Proc. 1997 Int. Conf. Very Large Data Bases (VLDB'97)*, pages 186–195, Athens, Greece, Aug. 1997.
- [ZRL96] T. Zhang, R. Ramakrishnan, and M. Livny. BIRCH: an efficient data clustering method for very large databases. In *Proc. 1996 ACM-SIGMOD Int. Conf. Management of Data (SIGMOD'96)*, pages 103–114, Montreal, Canada, June 1996.